

Search when Consumers are Loss Averse

Marco. A. Haan, Wim H. Siekman

Motivation

Literature

Search with differentiated products

Search and reference dependence

Solving

Results

Conclusion

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Consumer search and switching cost workshop Moscow, 2013

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Increased interest in Behavioral Economics

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- Identifying behavioral biases and incorporating them into formal models.
- If we want to understand how markets function, we have to take such biases into account.



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Increased interest from Antitrust Authorities

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- OFT (2010), What does Behavioural Economics mean for Competition Policy?
- Oxera (2013), Behavioural economics and its impact on competition policy; A practical assessment with illustrative examples from financial services (for Dutch ACM)
- Potentially important policy implications.
- If biases lead to higher prices (and if higher prices imply lower welfare) there may be scope for policy intervention.



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- We look at one specific, particularly well-documented bias: loss aversion (aka reference-dependence or gain-loss utility).
- Kahnemann and Tversky (Ectr 1979).
- If people get less than they expected, they suffer additional disutility.
- If you expect x, but you get y < x, your utility is $y \lambda(x y), \ \lambda > 0.$
- In paper also: additional utility if you get more than you expect: if y > x, utility is $y + \gamma \lambda(y x), 0 < \gamma < 1$.

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How to model this!?

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- Köszegi and Rabin (QJE 2006): Personal equilibrium.
- Behavior has to be consistent with expectations.
- If a random variable affects decisions, gain and loss utility are evaluated against all possible realizations of that random variable, weighed by their likelihood.
- So if you expect some $x \sim U[0,1]$, you get y, utility is $y \lambda \int_x^1 (\chi y) d\chi$.



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Applications in IO

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- Notably: Heidhues and Köszegi (AER 2008). Salop circle. Loss aversion weakly increases prices.
- Karle and Peitz (RAND; forthcoming).
- Zhou (JEMS 2012) in the context of search, 2 firms, first is reference point.



Fix thoughts: Heidhues and Köszegi (simplified)

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- Hotelling line, A at 0, B at 1.
- Crucial assumption: disappointment utility is separable in price and product dimension.
- Reference point: equilibrium outcome.
- Suppose firm A defects from tentative equilibrium.
- Downward: marginal guy moves to the right, is disappointed about product if he buys A.
- Upward: marginal guy moves to the left, is disappointed about price if he buys A, but is disappointed about product if he buys B.

- Kink in profit function at tentative equilibrium.
- Continuum of price equilibria.



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- Consumers observe all offers simultaneously.
- More natural: disappointed by the offer of the particular firm you're currently visiting.
- Hence we incorporate it in a model of sequential search and differentiated products.
- What is the effect of consumer loss aversion on equilibrium prices?
- A priori: unclear.
 - More reluctant to continue searching.
 - More easily disappointed by an offer.



Search with differentiated products

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• A single consumer has utility $u(p_i) = v + \varepsilon_i - p_i$ when buying from firm i.

- Match values $\varepsilon_i \sim F$, with 1 F log-concave.
- Firms cannot observe ε_i , the consumer does not know them in advance.
- Sequential search (for match values and prices)
- Searches cost *s* per shop.
- Firms are visited randomly.
- Covered market.
- Perfect recall.
- Infinitely many firms.



The search decision

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• At equal prices, expected benefits from search when current best match is *x*:

$$b(x) = \int_x^\infty (\varepsilon - x) f(\varepsilon) d\varepsilon$$

- Implicitly define $\hat{\varepsilon}$ by $b(\hat{\varepsilon}) = s$.
- In equilibrium, consumers continue search whenever $\varepsilon < \hat{\varepsilon}$.

• Probability of additional search: $F(\hat{\varepsilon})$.



Equilibrium pricing

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- Suppose a firm defects to some p_i .
- A consumer that visits i still buys if $\varepsilon_i > \hat{\varepsilon} p_i + p^*$.
- This allows us to write down expected profits for such a defector.
- Maximizing profits and imposing symmetry yields p^* .
- Equilibrium price: $p^* = \frac{1 F(\hat{x})}{f(\hat{x})}$, for uniform: $\sqrt{2s}$.

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Including reference dependence

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will affect utility in 3 dimensions:

- **1** Price dimension.
- 2 Match value dimension.
- **3** Search cost dimension.
 - Crucial assumption: disappointment utility is separable in these three dimensions.



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Solution strategy

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- Fix a value of *ε̂*.
- Derive implications.
- Find the value of $\hat{\varepsilon}$ that is consistent with optimal search behavior while taking possible disappointments into account: $\hat{\varepsilon}_L$.
- Feed that into the firms' maximization problem.
- Loss aversion in match and search dimension will affect $\hat{\varepsilon}_L$.

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• Given $\hat{\varepsilon}_L$, loss aversion in price dimension will affects firms' problem.



The Price Dimension

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- Consumers take equilibrium price as reference point.
- Hence they are disappointed if they find a firm that defects by setting a higher price.
- Kinked profit function, continuum of equilibria.



The Match Value dimension

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We can consider three possibilities:

- **1** Take current best match as reference point.
- 2 Take what he expects at this firm as a reference point.
- **3** Take the match value she ends up with in equilibrium as reference point.
 - The first is analytically intractable, as it yields non-stationary cut-off points.
 - The third seems most consistent with personal equilibrium.

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• The second yields the same qualitative results.



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The Match Value Dimension (ctd)

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• For a given $\hat{\varepsilon}$, *H* is the distribution from which the consumer expects draw her realized match value:

$$H(\xi) = \Pr\left(\varepsilon < \xi | \xi > \hat{\varepsilon}\right) = \frac{\int_{\hat{\varepsilon}}^{\infty} dF\left(\xi\right)}{1 - F\left(\hat{\varepsilon}\right)}.$$

• Post-disappointment match value, for $\varepsilon \geq \hat{\varepsilon}$

$$\varepsilon_L(\varepsilon) = \varepsilon - \lambda \int_{\varepsilon}^{\infty} (\tau - \varepsilon) dH(\tau)$$

Otherwise

$$\varepsilon_{i} - \lambda \int_{\hat{\varepsilon}}^{\infty} (\tau - \varepsilon_{i}) dH(\tau) = \varepsilon_{i} - [E(\varepsilon|\varepsilon > \hat{\varepsilon}) - \varepsilon_{i}]$$

• This defines a new "adapted match value" ε_L with distribution G.



The Search Cost Dimension

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- A priori expected to continue search when $\varepsilon < \hat{\varepsilon}$.
- Disappointment: $\lambda \int_{\hat{\varepsilon}}^{1} s dx$.
- Hence, adapted search costs:

$$s_L = s + s\lambda[1 - F(\hat{\varepsilon})]$$

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• Technical note: in fact, you should do this with the distribution of expected number of searches. That gives the same result.



Solving for consumer behavior

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- Finding the cut-off point $\hat{\varepsilon}_L$ now involves equating

$$\int_{\hat{\varepsilon}}^{\infty} (\varepsilon_L(\varepsilon) - \varepsilon_L(\hat{\varepsilon})) f(\varepsilon) d\varepsilon = s + s\lambda [1 - F(\hat{\varepsilon})]$$

with

$$\varepsilon_L(\varepsilon) = \varepsilon - \lambda \int_{\varepsilon}^{\infty} (\tau - \varepsilon) dH(\tau)$$

and

$$H(\xi) = \Pr\left(\varepsilon < \xi | \xi > \hat{\varepsilon}\right) = \frac{\int_{\hat{\varepsilon}}^{\infty} dF\left(\xi\right)}{1 - F\left(\hat{\varepsilon}\right)}.$$

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- This is a tough problem.
- Tractable if F is uniform.



Solving the Model (ctd)

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- Once $\hat{\varepsilon}_L$ is derived, the firms' problem is similar to before.
- However, firms do have to additionally take into account that defecting from a tentative equilibrium to a higher price yields disappointed consumers that are hence more likely to walk away.



Results

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- Continuum of equilibrium prices; upper bound is increasing in λ, lower bound is decreasing in λ if s is small enough.
- So equilibrium prices may be decreasing in λ !:
- In the search dimension: higher prices (searching becomes more costly).
- In the price dimension: weakly lower prices (consumers are more sensitive).
- In the match value dimension: higher prices (more product differentiation).



Results (ctd)

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- Consumers search more, hence settle for less.
- Prices increase in search costs and decrease in the number of firms.

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- We added reference dependence to a model of consumer search with differentiated products.
- Doing so yields more search.
- Prices may increase or decrease.