Markets for Ideas, Asymmetric Information and the Allocation of Managerial Skills*

Hendrik Hakenes[†] University of Bonn Martin Peitz[‡]
University of Mannheim

June 3, 2011

Abstract

The success of a product is often jointly determined by the usefulness of an idea and managerial skill, which are in a complementary relationship. We postulate that consumers and incoming managers cannot observe these sources of success, but rely on profit data to form their beliefs. Incoming managers take over firms, replace outgoing managers, and acquire ideas. The sales price of an idea increases with the prior to purchase unobservable usefulness of an idea. Though managerial skills are endogenously positively correlated over time, useful ideas end up under the control of better skilled managers. The market for ideas leads to positively assortative matches even though asymmetric information constitutes a friction in the matching of ideas and managers.

Keywords: Allocation of ideas, innovation, entrepreneurship, asymmetric information, ownership change, reputation transfer.

JEL-classification: L14, L15, G34.

^{*}We thank Martin Hellwig, Nicola Persico, participants of the EEA, and seminar participants in Mannheim for discussion and input. All remaining errors are our own.

[†]University of Bonn, Adenauerallee 24-42, D-53113 Bonn, Germany, hakenes@uni-bonn.de.

[‡]Department of Economics, University of Mannheim, L7 3-5, 68131 Mannheim, Germany, martin.peitz@googlemail.com.

1 Introduction

On November 13, 2006, Google acquired YouTube for \$1.65 billion. YouTube had only been founded in February 2005. Soon after the acquisition, both the monthly growth and the market share of YouTube video views overtook that of competitors (see figure 1). YouTube's revenues in 2007 were not material. But soon after the acquisition, YouTube started to show commercials before regular videos. For 2012, CitiBank estimates revenues at \$1 billion.

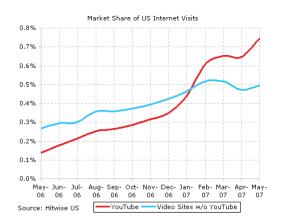


Figure 1: Growth of YouTube Market Share

Has Google been lucky? We develop a theory of idea trading that suggests that the result may only partly be attributable to luck. The other part stems from a better match of ideas and managerial skill since a successful combination of idea and managerial skill is needed for firms to prosper. When planning the deal, Google could rely on publicly available information. But it is due to the institution of a market for ideas that firm performance improved. The rents that are generated through the rematching are partly transferred to the owner of the idea.

In this paper we develop a theory of idea trading under asymmetric information. To fix ideas, initially there is an innovator (in the example, YouTube) who also acts as a manager. After some period, ideas are offered for sale. We do not require that innovators lack managerial skills, but postulate that a good innovator is not necessarily a good manager. In addition, we postulate that there is a complementary relationship between the usefulness of an idea and managerial skill: It is better for society that a good idea is skillfully managed and a bad idea less so than the reverse. Idea and managerial skill are complements, jointly determining the consumer valuation of a product. A reallocation of managerial skill and ideas is therefore efficiency increasing and ideas are sold to managers (in the example, to Google).

Given the complementary relationship, highly skilled managers would like to purchase good ideas; less skilled managers are left with worse ideas. However, immediate

perfect sorting requires that incoming managers perfectly observe the usefulness of an idea. Under perfect observability, the managerial skill of the innovator would be immaterial to the allocation after the market for ideas has cleared. More realistically, as we consider in this paper, the usefulness of an idea is unobservable to outsiders, i.e. consumers of the product and incoming managers who are the potential buyer of the idea. It appears to be an open question how the right combination of ideas and skills are formed over time under asymmetric information.

Outsiders only observe profits from the previous period and can try to make inferences from this observation. In market equilibrium, highly skilled managers acquire firms with successful products in the previous period. Since high profits in the previous period are more likely to have been resulted from an innovator with high managerial skills, skills of predecessors and successors are positively correlated. Furthermore, a better idea sells at a higher price. In a sense, the reputation of the innovator is transferred to the succeeding manager.

Let us look at the argument in more detail: We have to understand both the product market and the market for ideas. After a new product is released on the market, customers can judge its usefulness. However, a failure of the product does not necessarily imply that the underlying technology is not appropriate. The failure may rather be due to insufficient managerial skills of the innovator. This means that consumers face a signal extraction problem since they only observe the overall performance of the product. The start-up is then taken over by an investor who has the same information as customers. This investor obtains access to the innovator's idea and contributes with his own managerial skills, or appoints his own managers. While we may have some faith in the active screening role of the incoming investor cum manager (i.e., his expertise to judge the merits of a new technology) we take a more sceptical approach and ask whether the market system as such provides a (possibly imperfect) self-selection mechanism that improves upon the initial combination of idea and managerial skill. We may attribute higher average managerial skills to incoming investors/managers vis-à-vis outgoing innovators; however, we believe it is important to show that a better allocation due to a more productive input combination is the outcome of sorting in market equilibrium and not simply due to a better distribution of incoming managers.

After the transfer of ownership to the incoming manager, consumers are offered a new product which results from the combination of the previously developed idea and current managerial skills. Consumers repeatedly purchase (or there is some word-of-mouth between consumers) allowing them to update their beliefs after purchase. While low-skilled managers taking over successful ideas are initially not detected, repeat purchases rely on previous experience which is linked to the underlying type of the manager. This gives stronger incentives for skilled incoming managers to take over those start-ups that showed a good performance. Since initial good performance relies not only on the technology but also on the managerial skills of the innovator, this skill is valuable to the innovator as it affects the price paid by the acquiring investor cum manager. Hence, (because of the signal extraction problem)

in market equilibrium there is a positive correlation between the managerial skill of the innovator and the manager, although this managerial skill is initially unrelated to the "quality" of the idea. Also there is a positive correlation between technology and the managers' skill. This shows that the market mechanism improves on the initial allocation, but does not implement the first best. While the initial allocation is characterized by random matching between technology and managerial skills, the situation after ownership change is characterized by positive assortative matching.

We consider a model in which a firm is sold after the first period, and the usefulness of the idea is not revealed, but can only partially inferred from product performance. Our findings are as follows:

- 1. After the sale of the firm there is a positive correlation between managerial skill from period 1 onward and the quality of the technology.
- 2. The managerial skill in period 0 positively affects the sale price of the firm although it does not affect future performance.
- 3. There is a positive correlation between managerial skills in periods 0 and 1.
- 4. The sale of firms improves on the initial allocation and increases social welfare.

The first finding is not specific to our model. This positive correlation would even hold if incoming managers learnt the quality of the technology directly before deciding whether to buy the firm. However, in a world in which the quality of the technology becomes publicly known, there is no role for managerial skills in period 0 to affect future allocations. It thus would not affect the sale price of the firm. Thus, our second finding is due to our assumption of asymmetric information. The underlying argument is that more managerial skills make good performance more likely. Due to the signal extraction problem this makes consumers trust the used technology and therefore the innovator's technology becomes more valuable. The lack of full information also lies at the heart of our third finding. An initial owner with higher skills will produce better products in expectations. Consumers observe only the product's performance, not the innovator's managerial skills. Therefore, they attribute some of that performance to the usefulness of the idea. But incoming managers, when deciding which firm to buy, prefer more useful ideas. The higher their own skills, the higher their willingness to pay for good ideas. As a consequence, better managers end up buying better performing firms, which tend to be firms that are initially run by high-skill innovators. With respect to the social desirability of the trade in firms, we note that initially ideas and managerial skills are matched randomly. Since all good ideas tend to be bought by highly skilled managers, ideas and managerial skills end up being partly assortatively matched, which increases social welfare because of the input complementarity.

The remainder of the paper is organized as follows. After a short literature review, the following section 2 introduces the base model. Section 3 characterizes and discusses the equilibrium with positively assortative matching on the market for firms. Section 4 contains some model extensions. Section 5 concludes.

Literature. Our paper introduces a mechanism how "reputation" can be transferred from a manager to his successor when a firm is sold. Hence, our paper is related to other work on reputation transfer. In the seminal paper by Tadelis (1999), consumers buy products from firms. The owners of firms change unobservedly, hence reputation does not evaporate immediately with the trade of a firm. This leads to (partial) sorting, which in effect leads to reputation transfer. By contrast, trading the firm is observable in our model, but one of the factors of production is a long-run factor. This also leads to partial sorting, and to reputation transfer.

Morrison and Wilhelm (2004) look at the incentives to pass on human capital within a firm. As a consequence, also the reputation will be passed on. This phenomenon is absent in our model. In Levin and Tadelis (2005), profit sharing between team members plus reputation pooling alleviates moral hazard problems, especially at the end of a manager's career. Also Bar-Isaac (2007) models teams, where the ability of each team member cannot be observed separately. Each member has thus an incentive to work hard, because this improves also the reputation of his team mates. At retirement, they can then sell out at a higher price. Also in our setting, the types of innovators and technologies can only jointly be determined. However, our focus is on the sorting properties of the equilibrium. In Hakenes and Peitz (2007), firms acquire a customer base over some time. But losing good customers is easy, hence on the market for firms, better managers have an incentive to bid more for better firms. Again, there is partial sorting and, as a consequence, reputation transfer. A key feature of that paper is that reputation is only local. Tadelis (2002) shows that a mechanism of reputation transfer increases incentives to work, even at the end of ones career. This augments ones own reputation, which can then be sold to the next generation. We obtain a related result in section 4.3. ¹ In contrast to previous work our paper considers the dynamics over a product's life cycle.

A different strand of related literature deals with the match between skilled managers and projects. For example, Gabaix and Landier (2008) hold the match between tasks and talent of CEOs responsible for the steep increase in CEO pay (before the crisis). Acharya, Pagano, and Volpin (2010) provide an example where skilled financial managers are matched to risky projects. If there is a mismatch, risk endogenously increases, possibly leading to crises.²

2 The Model

Consider an economy with three types of agents: innovators, entrepreneurs cum managers, and consumers. Innovators and managers use an idea; we may think of

¹Tadelis (2003) looks at prices for reputations, again in the context of reputation transfer. Andersson (2002) considers the transfer of reputation between products in the context of umbrella branding. The same applies for Hakenes and Peitz (2008), in a moral hazard problem.

²The list and discussion of literature expanded further. For example, Andersson, Freedman, Haltiwanger, and Shaw (2009) Abowd, Haltiwanger, Lane, McKinney, and Sandusky (2007) Baker, Gibbs, and Holmström (1993, 1994a,b); Baker and Holmström (1995) should be mentioned.

this as the technology of production. There are three dates $(t \in \{0, 1, 2\})$. In period t = 0, innovators produce and sell one unit to each consumer. At the beginning of period t = 1, innovators retire and sell their firm/idea to an entrepreneur cum manager.³ In t = 1 and t = 2 each, managers produce one unit of the redesigned product and sell it to consumers. All agents are risk neutral and have perfect recall, there is no discounting.

Innovators have different types S_0 , standing for the managerial quality they achieve. $\log S_0$ is normally distributed with mean 0 and variance σ_0^2 , thus type S_0 is lognormally distributed with $\log S_0 \sim N(0, \sigma_0^2)$. The mean of S_0 is hence $e^{\sigma_0^2/2}$. Innovators can produce in period t = 0, but not in t = 1 and t = 2.

Also managers have different types S_1 , standing for quality, which is lognormally distributed with $\log S_1 \sim N(0, \sigma_1^2)$. Managers can produce in period t = 1 and t = 2, but not in t = 0.

Finally, both innovators and managers must use an idea as a long-run factor, which we call technology. *Technologies* also come in different quality types T, lognormally distributed with $\log T \sim N(0, \tau^2)$. All random variables S_0, S_1 and T are stochastically independent.

In the production process, the types of innovators (or managers) and technologies are complements. If an innovator of type S_0 uses a technology of type T, the product quality is $Q = S_0 T$. If a manager of type S_1 uses technology T, the product quality will be $Q = S_1 T$.

Consumers have unit demand for the product in each period. There is a unit mass of consumers. Goods are experience goods; consumers cannot assess the quality before consumption. They demand one unit of the product if the price is equal or below its expected valuation, otherwise they demand zero.

We solve for perfect Bayesian equilibria. The market for firms, however, is competitive. Furthermore, firms are assumed to set retail prices such that they extract the full expected surplus of the consumers. The time line is given by table 1. An illustration of the main modeling ingredients and the timing is given in figure 2.

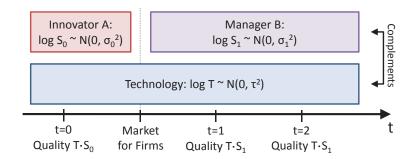
3 Equilibrium Characterization

The Product Market in Period t=0. At the beginning of that date, innovators and technologies are matched randomly. Because $\log S_0$ and $\log T$ both are normally distributed and stochastically independent, also $\log S_0 + \log T$ is normally distributed and variances are added up. Namely, $\log S_0 \sim N(0, \sigma_0^2)$ and $\log T \sim N(0, \tau^2)$,

³Note that this analysis also applies to take-over by other firms or investors who put a new manager in charge. In that case, we implicitly assume that the incentives of this firm or investor are perfectly aligned with the incentives of the new manager.

- 0 Innovators use the technology to produce one product and sell it to consumers. Consumers experience the product and update their beliefs.
 - Market for firms: Innovators announce prices P_0 for their firms/technologies, managers decide whether to buy.
- 1 Innovators use the technology to produce one product and sell it to consumers. Consumers experience the product and update their beliefs.
- 2 Innovators use the technology to produce one product and sell it to consumers. Consumers experience the product and update their beliefs.

Figure 2: Graphic Illustration of the Model



hence $\log(S_0 T) = (\log S_0 + \log T) \sim N(0, \sigma_0^2 + \tau^2)$. At date 0, the product quality $Q_0 = S_0 T$ is hence lognormally distributed, with an expected value of

$$E[Q_0] = e^{\frac{\sigma_0^2 + \tau^2}{2}}. (1)$$

Because consumers have unit demand, they will demand zero if the price exceeds the expected quality, otherwise they demand exactly one unit. The innovator sets the price at the expected valuation of consumers. Because there are no production costs and consumers are of unit mass, profits at date zero are

$$\Pi_0 = E[Q_0] = e^{\frac{\sigma_0^2 + \tau^2}{2}}. (2)$$

These profits depend neither on the managerial skill of the innovator S_0 nor on the quality of the technology T because both are not known to consumers at this date. This will change after date 0, when the product has been bought and consumed, and the quality $Q_0 = S_0 T$ has become publicly known.⁴ At the end of date 0,

⁴While some consumers may learn from their experience, the assumption here is that this information is made publicly available, e.g. by the publication of consumer reports.

the innovator sells the firm. Hence, the innovator's type will no longer be relevant for any firm, but the technology as the long-run factor remains important for the success of the product. Therefore, managers and consumers are concerned about the technology's type, which they may partially infer from the aggregate quality Q_0 , making use of Bayes' rule. Note that managers only care about the technology's type because consumers learn: The manager's willingness to pay for the firm depends on the expected profit the new firm is going to derive, which only depends on the consumers' valuations. Managers and consumers face the same signal extraction problem. This problem is tractable because the logs of S_0 , T and Q_0 are normally distributed. The expected value of T, given the information Q_0 is updated to

$$E[\log T | \log Q_0] = \frac{1/\sigma_0^2}{1/\sigma_0^2 + 1/\tau^2} \log Q_0 = \frac{\tau^2}{\sigma_0^2 + \tau^2} \log Q_0, \tag{3}$$

and the variance of T is updated to

$$V[\log T | \log Q_0] = \frac{1}{1/\sigma_0^2 + 1/\tau^2} = \frac{\sigma_0^2 \tau^2}{\sigma_0^2 + \tau^2}.$$
 (4)

How can we interpret these expression? If S_0 were known with certainty, i. e. $\sigma_0 = 0$, this would imply that $\log S_0 \sim N(0,0)$ and hence $\log S_0 = 0$, thus $S_0 = 1$. The expected value of $\log T$ would then be identical to $\log Q_0$, the product quality would perfectly reveal the type of the technology. Formally, $E[\log T|\log Q_0] = \log Q_0$. If, on the other hand, T were known with certainty, i. e. $\tau = 0$, this would imply that T = 1. Because T would already be known, nothing could additionally be learnt from the product quality Q_0 . Formally, $E[\log T|\log Q_0] = \log 1 = 0$. These are two limiting cases. Since the expected value of a lognormal distribution with parameters μ and σ is $e^{\mu + \sigma^2/2}$, the expected value of T conditioned on Q_0 is

$$E[T|Q_0] = \exp\left(\frac{\tau^2}{\sigma_0^2 + \tau^2} \left(Q_0 + \frac{\sigma_0^2}{2}\right)\right).$$
 (5)

The larger τ in relation to σ_0 , the more consumers and managers can learn on the quality type T from observing Q_0 .

The Firm Market before Period t = 1. At the end of period 0, the market for firms opens. In the assortative equilibrium, better new managers buy the firms with better signals Q_0 . Here, we only look at the consequences for the consumers' information. We will calculate the equilibrium price $P(Q_0)$ for a firm, depending on the observed product quality it has produced, further below.

The new managers' types are lognormally distributed, $\log B \sim N(0, \sigma_1^2)$. Slightly abusing notation, let $S_1(Q_0)$ denote the type of manager who buys a firm that has produced quality Q_0 . In the assortative equilibrium, $S_1(Q_0)$ is a strictly increasing function. Furthermore, because both $\log S_1$ and $\log Q_0$ are normally distributed, $\log S_1(\log Q_0)$ is a linear transformation of $\log Q_0$. This linear function must be such

that it maps the mean of $\log Q_0$ onto the mean of $\log S_1$, and it transforms the standard deviation of $\log Q_0$ into the standard deviation of $\log S_1$. Since signals Q_0 have standard deviation $\sqrt{\sigma_0^2 + \tau^2}$ and types of managers have standard deviation σ_1 , a firm with signal Q_0 will be mapped onto a manager with type

$$\log S_1(\log Q_0) = \frac{\sigma_1}{\sqrt{\sigma_0^2 + \tau^2}} \log Q_0, \text{ and thus}$$

$$S_1 = Q_0^{\frac{\sigma_1}{\sqrt{\sigma_0^2 + \tau^2}}}.$$
(6)

The mapping is derived under the assumption of assortative matching. This will have to be supported by a pricing function for firms, which we will be able to compute after knowing the product prices in period 1 and 2.

The Product Market in Period t=1. Each consumer is concerned about the probability distribution over quality Q_1 . What can he learn from the product performance in the previous period about T and S_1 ? Each consumer has consumed at date 0 and thus knows Q_0 . Therefore, he updates his beliefs about mean and variance of $\log T$ as in (4) and (3). Furthermore, because he knows that under assortative matching firms which performed better in period 0 are matched with more skilled managers at the end of date 0, he can infer S_1 from Q_0 making use of (6). Period 1 quality $Q_1|Q_0 = S_1|Q_0 \cdot T|Q_0$ will be distributed with

$$V[\log Q_1 | \log Q_0] = V(\log T | \log Q_0) = \frac{1}{1/\sigma_0^2 + 1/\tau^2} = \frac{\sigma_0^2 \tau^2}{\sigma_0^2 + \tau^2} \quad \text{and}$$

$$E[\log Q_1 | \log Q_0] = \left(\frac{\tau^2}{\sigma_0^2 + \tau^2} + \frac{\sigma_1}{\sqrt{\sigma_0^2 + \tau^2}}\right) \log Q_0 = \frac{\tau^2 + \sqrt{\sigma_0^2 + \tau^2} \sigma_1}{\sigma_0^2 + \tau^2} \log Q_0.$$
(8)

The new manager anticipates that consumers rationally hold these expectations and sets the price at which consumers are indifferent between buying and not buying. Because consumers' expectations are conditioned on Q_0 , the product price at date 1 will also be conditioned on Q_0 . Considering (8) and (7), profits at date t = 1 are

$$\Pi_1(Q_0) = E[Q_1|Q_0] = \exp\left(\frac{\tau^2 + \sqrt{\sigma_0^2 + \tau^2} \sigma_1}{\sigma_0^2 + \tau^2} \log Q_0 + \frac{1}{2} \frac{\sigma_0^2 \tau^2}{\sigma_0^2 + \tau^2}\right). \tag{9}$$

Here, the first fraction is due to the consumers' beliefs (τ^2) and the assortative matching $(\sqrt{\sigma_0^2 + \tau^2} \sigma_1)$, the second fraction is due to the variance.

The Product Market in Period t=2. After the product market at date 1, Q_1 is public information. In the base version of the model management changes only once throughout the time horizon and thus the manager remains in the firm after period 1. Then the expected quality at date 2 will simply be the quality at date 1, $Q_2 = Q_1 = S_1 T$. The manager will thus set the product price at Q_2 , and the profit equals this price, $\Pi_2 = S_1 T$.

Firm valuations in Period t = 1. A manager who buys a firm that has produced quality Q_0 will earn Π_1 and Π_2 during the next periods. We can thus calculate his willingness to pay for such a firm, and thus calculate prices on the market for firms in equilibrium. Let $P_0(Q_0)$ denote the price investors pay in equilibrium for a firm to innovators, which depends on the public signal $Q_0 = S_0 T$ at date 0. Then the expected profit of a manager of type S_1 is

$$\Pi_{1} + E[\Pi_{2}] - P_{0}(Q_{0}) = \exp\left(\frac{\tau^{2} + \sqrt{\sigma_{0}^{2} + \tau^{2}} \sigma_{1}}{\sigma_{0}^{2} + \tau^{2}} \log Q_{0} + \frac{1}{2} \frac{\sigma_{0}^{2} \tau^{2}}{\sigma_{0}^{2} + \tau^{2}}\right)
+ B \cdot \exp\left(\frac{\tau^{2}}{\sigma_{0}^{2} + \tau^{2}} \log Q_{0} + \frac{1}{2} \frac{\sigma_{0}^{2} \tau^{2}}{\sigma_{0}^{2} + \tau^{2}}\right) - P_{0}(Q_{0}).$$
(10)

It must be optimal for the manager to pay the price P_0 for the firm. Which manager S_1 will buy a firm that has produced quality Q_0 ? In (6), we have argued that S_1 is a monotonic function of Q_0 . Quality Q_0 is "designated" for type S_1 with

$$S_1 = Q_0 \frac{\sigma_1}{\sqrt{\sigma_0^2 + \tau^2}}. (11)$$

In an assortative matching equilibrium, the pricing function $P_0(Q_0)$ should be such that type S_1 optimally chooses quality Q_0 . Thus, considering the first-order condition, the marginal expected profit from a firm that has produced quality Q_0 must vanish,

$$0 = \frac{\tau^2 + \sqrt{\sigma_0^2 + \tau^2} \,\sigma_1}{\sigma_0^2 + \tau^2} \exp\left(\frac{\sqrt{\sigma_0^2 + \tau^2} \,\sigma_1 - \sigma_0^2}{\sigma_0^2 + \tau^2} \log Q_0 + \frac{1}{2} \frac{\sigma_0^2 \,\tau^2}{\sigma_0^2 + \tau^2}\right) + \frac{\tau^2}{\sigma_0^2 + \tau^2} S_1 \cdot \exp\left(-\frac{\sigma_0^2}{\sigma_0^2 + \tau^2} \log Q_0 + \frac{1}{2} \frac{\sigma_0^2 \,\tau^2}{\sigma_0^2 + \tau^2}\right) - P_0'(Q_0). \tag{12}$$

Consequently, we must substitute (11) into (12), which yields

$$P_0'(Q_0) = \frac{\tau^2 + \sqrt{\sigma_0^2 + \tau^2} \,\sigma_1}{\sigma_0^2 + \tau^2} \exp\left(\frac{\sqrt{\sigma_0^2 + \tau^2} \,\sigma_1 - \sigma_0^2}{\sigma_0^2 + \tau^2} \log Q_0 + \frac{1}{2} \frac{\sigma_0^2 \,\tau^2}{\sigma_0^2 + \tau^2}\right) + \frac{\tau^2}{\sigma_0^2 + \tau^2} Q_0 \sqrt[\sigma_0^2 + \tau^2} \cdot \exp\left(-\frac{\sigma_0^2}{\sigma_0^2 + \tau^2} \log Q_0 + \frac{1}{2} \frac{\sigma_0^2 \,\tau^2}{\sigma_0^2 + \tau^2}\right). \tag{13}$$

This differential equation must apply for the function $P_0(Q_0)$. If we can additionally identify one point Q_0 where we know the price $P_0(Q_0)$, we have a classical initial value problem and can solve for the complete function $P_0(Q_0)$.

For the worst quality $\log Q_0 = -\infty$, hence $Q_0 = 0$, the price must be $P_0(0) = 0$. This is seen as follows: According to (6), the associated manager type is $\log S_1 = -\infty$, hence $S_1 = 0$. This worst possible type does not have an incentive to pay anything for any technology because $S_1 T$ is always zero. He will never make any money at date t = 2, and he will buy the worst Q_0 , hence he cannot sell at a positive product price at date t = 1.

We can now integrate both sides of (13) and explicitly solve for the pricing function

$$P_{0}(Q_{0}) = \int_{0}^{Q_{0}} \left[\frac{\tau^{2} + \sqrt{\sigma_{0}^{2} + \tau^{2}} \sigma_{1}}{\sigma_{0}^{2} + \tau^{2}} \exp\left(\frac{\sqrt{\sigma_{0}^{2} + \tau^{2}} \sigma_{1} - \sigma_{0}^{2}}{\sigma_{0}^{2} + \tau^{2}} \log Q + \frac{1}{2} \frac{\sigma_{0}^{2} \tau^{2}}{\sigma_{0}^{2} + \tau^{2}} \right) + \frac{\tau^{2}}{\sigma_{0}^{2} + \tau^{2}} Q^{\frac{\sigma_{1}}{\sqrt{\sigma_{0}^{2} + \tau^{2}}}} \cdot \exp\left(-\frac{\sigma_{0}^{2}}{\sigma_{0}^{2} + \tau^{2}} \log Q + \frac{1}{2} \frac{\sigma_{0}^{2} \tau^{2}}{\sigma_{0}^{2} + \tau^{2}} \right) dQ$$

$$= \exp\left[\left(\frac{1}{2} \frac{\sigma_{0}^{2} \tau^{2}}{\sigma_{0}^{2} + \tau^{2}}\right) \left(\frac{\tau^{4}}{(\sigma_{0}^{2} + \tau^{2}) + (\tau^{2} + \sigma_{1} \sqrt{\sigma_{0}^{2} + \tau^{2}})} + 1\right) \right] Q_{0}^{\frac{\tau^{2} + \sigma_{1} \sqrt{\sigma_{0}^{2} + \tau^{2}}}{\sigma_{0}^{2} + \tau^{2}}}.$$

$$(14)$$

With this pricing function, one can immediately show that a manager of type S_1 does not benefit from buying a firm different from $S_1(Q_0)$ as given in (6).

Summary: Equilibrium Characterization. Summing up, we have shown that the price function $P_0(Q_0)$ constitutes a market equilibrium in which there is imperfect sorting. This is summarized by the following proposition.

Proposition 1 There is an equilibrium with imperfect sorting in which the equilibrium value of firms traded at the end of period 0 is given by (14).

Proof of proposition 1: In our equilibrium, there is imperfect sorting because better managers buy firms with better quality, which tend to be founded by better innovators. Hence, it suffices to show that the first-order approach also fulfills the second-order condition, to see that the behavior of buyers is indeed optimal. Indeed, inserting (14) into (10), taking the second derivative with respect to Q_0 , and respecting (11) yields

$$-\frac{\sigma_1 \tau^2}{\sqrt{\sigma_0^2 + \tau^2}^5} \exp\left(\frac{\sigma_0^2 \tau^2}{2(\sigma_0^2 + \tau^2)}\right) Q_0^{\frac{\tau^2}{\sigma_0^2 + \tau^2} + \frac{\sigma_1}{\sqrt{\sigma_0^2 + \tau^2}} - 2}$$
(15)

as the second derivative. This is clearly negative.

The firm price depends on the produced quality Q_0 : A higher observed quality Q_0 always leads to a higher price P_0 . Since more skills in period 0 have a positive effect on Q_0 , this established finding 2 of the introduction.

We are interested in the question whether "reputation" can be transferred from one generation of managers to the next. Put differently, are firms from better innovators likely to be bought by better managers? This question can be answered from two different perspectives. First, one can consider the correlation of S_0 and S_1 , of the types of innovator and manager. However, the reputation of the innovator is the innovator's type S_0 expected by consumers, conditioned on the observed quality Q_0 ,

and the manager's type S_1 expected by consumers, conditioned on the fact that the manager buys a firm with signal Q_0 . The second perspective is thus to consider the conditional correlation. Let us start with the second perspective. The prior distribution of S_0 is $\log S_0 \sim N(0, \sigma_0^2)$. In analogy to (3) and (4), after a consumer has observed the quality Q_0 , he updates the distribution to

$$\log S_0 |\log Q_0 \sim N\left(\frac{\sigma_0^2}{\sigma_0^2 + \tau^2} Q_0, \frac{\sigma_0^2 \tau^2}{\sigma_0^2 + \tau^2}\right). \tag{16}$$

The firm will then be bought by a manager with type S_1 as defined in (6). Therefore, the sorting between an innovator's logged reputation and the succeeding manager's expected logged ability is *perfect*. Now let us come back to the first perspective. What is the correlation between S_0 and S_1 , or equivalently, between $\log S_0$ and $\log S_1$? The correlation between $\log S_1$ and $\log Q_0$ is perfect, consequently

$$\rho(\log S_0, \log S_1) = \rho(\log S_0, \log Q_0) = \frac{\sigma_0^2}{\sigma_0 \sqrt{\sigma_0^2 + \tau^2}} = \frac{1}{\sqrt{1 + \tau^2/\sigma_0^2}}.$$
 (17)

In the limiting case of $\tau \to 0$, the correlation converges to one. If the information on T is rather precise, then Q_0 is nearly perfectly correlated with S_0 . But still, managers with a higher S_1 buy firms with a higher initial quality Q_0 . This means that good ideas are likely to be acquired by good managers. In the limiting case of $\sigma_0 \to 0$ or, equivalently, $\tau \to \infty$, the correlation converges to zero. If technology qualities are widely spread, then the signal Q_0 is heavily influenced by T, and relatively less influenced by S_0 . Because of the noise, the correlation between innovator and manager types goes becomes low. Still, better managers buy firms with better qualities Q_0 and hence in a first-order stochastic dominance sense those with better skilled innovators (higher S_0). This establishes the following proposition:

Proposition 2 Managerial skills in periods 0 and 1 are positively (but not perfectly) correlated.

Proposition 2 reflects finding 3 of the introduction. Since S_1 is an increasing function in Q_0 and there is a positive correlation between $\log T$ and $\log Q_0$, there is also a positive correlation between $\log T$ and $\log S_1$. This establishes finding 1 of the introduction. As we noted in the introduction, finding 1 is also preserved in a market in which asymmetric information is absent.

Comparative statics. The influence of the parameters σ_0 , σ_1 and τ is more complex, however. The following findings are based on numerical calculations, they illustrate the influence of these parameters. For comparability, the blue curve has the parameters $\sigma_0 = 1$, $\sigma_1 = 1$ and $\tau = 1$ in all three figures reported below. Then in each figure, a different parameter is changed.

Figure 3 shows $P_0(Q_0)$ for different variances of $\log S_0$, with $\sigma_0 \in \{1, 2, 4\}$. The dashed curves give the limiting cases $\sigma_0 \to 0$ and $\sigma_0 \to \infty$. If the dispersion of S_0 is extremely wide $(\sigma_0 \to \infty)$, then the quality Q_0 contains no information on the technology T. The product prices will not depend on Q_0 . Therefore, the price for all firms is identical, $P_0 = e^{\tau^2/2}$. In the other extreme, if $\sigma_0 \to 0$, the type of the innovator is known, and the quality Q_0 perfectly reveals the technology type T, and the firm price reacts sensitively to the observed quality Q_0 . For reaction of the firm price on σ_0 is ambiguous. If the observed quality is poor and Q_0 is small, then a large σ_0 obfuscates the information on T and thus has a positive impact on the price P_0 . The opposite is true for a larger observed quality Q_0 .

 $P_0(Q_0)$ $\begin{array}{c}
5 \\
4 \\
3 \\
2
\end{array}$

1.0

1.5

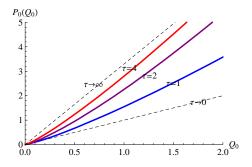
0.5

Figure 3: Effect of σ_0 on the Firm Price

Figure 4 shows $P_0(Q_0)$ for different variances of $\log T$, with $\tau \in \{1, 2, 4\}$. The dashed curves give the limiting cases $\tau \to 0$ and $\tau \to \infty$. For $\tau \to 0$, the pricing function becomes $P_0(Q_0) = Q_0^{\sigma_1/\sigma_0}$. For the limit $\tau \to \infty$, it becomes $P_0(Q_0) = 2 e^{\sigma_0^2/2} Q_0$. A comparison shows that the curve for $\tau \to \infty$ does not lie unambiguously above or below the curve for $\tau \to 0$. In general, the price therefore depends ambiguously on τ . Thus, τ influences P_0 in several ways. First, if τ is large, then the variance of T increases. It thus pays for managers to bid aggressively for firms in order not to end up with a bad quality. But second, as τ increases, the expected T also increases, hence the expected T0 also increases. The same T0 in a lower quantile if the distribution for larger T1. A T2 that is a medium quality for low T3 may be an extremely bad quality for larger T3. Consequently, worse managers will aquire such a firm and the price that is paid for the firm will be lower. Figure 3 shows that the first channel may dominate, but this does not hold for all parameter constellations.

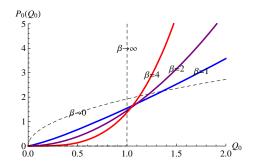
Finally, figure 5 shows $P_0(Q_0)$ for different variances of $\log S_1$, with $\sigma_1 \in \{1, 2, 4\}$. The dashed curves give the limiting cases $\sigma_1 \to 0$ and $\sigma_1 \to \infty$. For $\sigma_1 \to 0$, the function is proportional to a root of Q_0 ; for $\sigma_1 \to \infty$, it is zero for $Q_0 < 1$ and infinite for $Q_0 > 1$. In between, P_0 increases in σ_1 for small qualities Q_0 , and id decreases in σ_1 for larger qualities, with the following intuition. For a larger σ_1 , there are more good managers with high skills, but also more worse managers with low skills. Due to the complementarity with their own skills, low-skilled managers will bid less for a firm with fixed technology. On the other hand, high-skilled managers bid more.

Figure 4: Effect of τ on the Firm Price



This explains why, for higher σ_1 , the curves moves down on the left side, and moves up on the right side.

Figure 5: Effect of σ_1 on the Firm Price



Welfare. Especially when we want to compare the equilibrium with other scenarios, the welfare perspective will be interesting. In the welfare function, the transfer price $P(Q_0)$ cancels out because it is a mere transfer. Consumers pay exactly for the expected quality of products, hence their rent is zero. Thus, welfare consists only of the firm's profits. But firms have zero costs, thus welfare consists only of the firms' revenues. Finally, because the volume of products is fixed to one, welfare is identical to the sum of product prices from an ex-ante perspective,

$$W = \Pi_0 + E_0[\Pi_1] + E_0[\Pi_2] = \Pi_0 + 2 E_0[\Pi_1]$$

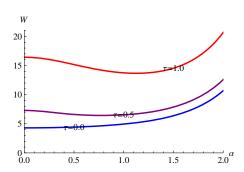
$$= \exp\left(\frac{\sigma_0^2 + \tau^2}{2}\right) + 2 E_0 \left[\exp\left(\frac{\tau^2 + \sqrt{\sigma_0^2 + \tau^2} \sigma_1}{\sigma_0^2 + \tau^2} \log Q_0 + \frac{1}{2} \frac{\sigma_0^2 \tau^2}{\sigma_0^2 + \tau^2}\right)\right]. \quad (18)$$

Now because $\log Q_0$ is normally distributed with mean 0 and variance $\sigma_0^2 + \tau^2$,

$$W = \exp\left(\frac{1}{2}(\sigma_0^2 + \tau^2)\right) + 2\exp\left(\frac{1}{2}(\sigma_1^2 + \tau^2) + \frac{\sigma_1 \tau^2}{\sqrt{\sigma_0^2 + \tau^2}}\right).$$
(19)

We note that welfare is increasing in σ_1 and τ , but not necessarily in σ_0 . The reason is, as mentioned above, that a larger σ_0 raises prices at date t=0, but also creates noise in the sorting process. For large σ_0 , the first effect always dominates, but for small σ_0 , the second effect can be dominant, depending on parameters σ_1 and τ . In figure 6, the welfare function is plotted for parameters $\sigma_1 = 1$ and $\tau \in \{0, 0.5, 1\}$, illustrating the possible non-monotonicity of W in σ_0 .

Figure 6: Welfare



For a welfare comparison, it is useful to consider as a benchmark a variation of the model where the firm is not sold at all. As we have shown, the market for firms is used to improve the sorting between technologies and managers. Hence, without the market and without sorting, the benefits from the complementarities will be smaller and welfare will be lower, provided that skills in the two periods are chosen from the same distribution. The equilibrium is straightforward. On the product market at date 0, the price will be $\Pi_0 = \exp((\sigma_0^2 + \tau^2)/2)$. After t = 0, the quality Q_0 is revealed. Because the firm is not sold, the quality will stay at Q_0 for the next periods, hence the price at t = 1 and t = 2 will be Q_0 . Taking expectations from date 0, expected prices are $E_0[\Pi_1] = E_0[\Pi_2] = \Pi_0 = \exp((\sigma_0^2 + \tau^2)/2)$. Welfare thus amounts to

$$W = \Pi_0 + E_0[\Pi_1] + E_0[\Pi_2] = 3 \exp\left(\frac{\sigma_0^2 + \tau^2}{2}\right). \tag{20}$$

A comparison with (19) shows that the interim market improves welfare iff

$$\sigma_1 > \frac{\sqrt{\sigma_0^4 + \sigma_0^2 \tau^2 + \tau^4} - \tau^2}{\sqrt{\sigma_0^2 + \tau^2}},\tag{21}$$

which again is smaller than σ_0 . Because $E[S_0] = \exp(\sigma_0^2/2)$ and $E[S_1] = \exp(\sigma_1^2/2)$, the above condition has the following interpretation. If $\sigma_1 = \sigma_0$, i.e. if the skill distribution of new managers is the same as the one of innovators, creating a market for IPOs or takeovers always improves welfare because it leads to better matches and therefore achieves the benefits of the complementarity between managers and technologies. However, if $\sigma_0 \geq \sigma_1$ such that (21) held, innovators could do the job better than managers on average. Then introducing the sales of firms after period 0 would reduce welfare.

4 Extensions

4.1 Observability of the Idea

As a first modification, we consider a model where the type of technology or idea T is perfectly revealed before the market for firms operates.

At date 0, the price will depend only on S_0 and T, and T is not yet revealed. Thus, as before, the price on the product market will equal the expected quality and the period profit is $\Pi_0 = e^{(\sigma_0^2 + \tau^2)/2}$. When the product is consumed, both T and S_0 are revealed. In an assortative equilibrium, better managers with higher B will buy firms with better qualities, higher T. Because $\log S_1$ has standard deviation σ_1 and $\log T$ has standard deviation τ , the mapping is straightforward,

$$\log S_1(\log T) = \frac{\sigma_1}{\tau} \log T, \quad \text{thus} \quad S_1 = T^{\sigma_1/\tau}. \tag{22}$$

At date 1, consumers pay the expected quality for the good. For a firm of type T, they expect it has been bought by a manager of type $S_1 = T^{\sigma_1/\tau}$, hence the expected quality is $T \cdot T^{\sigma_1/\tau} = T^{1+\sigma_1/\tau}$, and thus $\Pi_1 = T^{1+\sigma_1/\tau}$. At date 2, both T and S_1 are known, and $\Pi_2 = S_1 T$. We can thus calculate expected profits for a manager, net of the firm's price,

$$\Pi_1 + \Pi_2 - P_0(T) = T^{1+\sigma_1/\tau} + S_1 T - P_0(T). \tag{23}$$

The first-order condition yields

$$P_0'(T) = \frac{\tau + \sigma_1}{\tau} T^{\sigma_1/\tau} + S_1. \tag{24}$$

Substituting (22), bearing in mind that $P_0(0) = 0$ and integrating yields

$$P_0'(T) = \frac{\tau + \sigma_1}{\tau} T^{\sigma_1/\tau} + T^{\sigma_1/\tau} = \frac{2\tau + \sigma_1}{\tau} T^{\sigma_1/\tau},$$

$$P_0(T) = \int_0^T \frac{2\tau + \sigma_1}{\tau} \tilde{T}^{\sigma_1/\tau} d\tilde{T} = \frac{2\tau + \sigma_1}{\tau + \sigma_1} T^{\frac{\tau + \sigma_1}{\tau}}.$$
(25)

To calculate welfare under perfect observability we need to aggregate the expected prices of products,

$$W = \Pi_0 + E_0[\Pi_1] + E_0[\Pi_2] = \Pi_0 + 2 E_0[\Pi_1]$$

$$= \exp\left(\frac{\sigma_0^2 + \tau^2}{2}\right) + 2 E_0\left[\exp\left(\frac{\tau + \sigma_1}{\tau}\log T\right)\right]$$

$$= \exp\left(\frac{\sigma_0^2 + \tau^2}{2}\right) + 2 \exp\left(\frac{(\sigma_1 + \tau)^2}{2}\right). \tag{26}$$

Comparing this welfare function with that of section 3, we obtain that perfect observability of the type of technology or idea T increases welfare. This is hardly

surprising since this will lead to perfect matches between T and S_1 from period 1 onward, which is not the case if the idea is not observable after period 0. Formally this is confirmed by comparing (19) with (26),

$$\exp\left(\frac{1}{2}(\sigma_{1}^{2} + \tau^{2}) + \frac{\sigma_{1}\tau^{2}}{\sqrt{\sigma_{0}^{2} + \tau^{2}}}\right) < \exp\left(\frac{(\sigma_{1} + \tau)^{2}}{2}\right),$$

$$\frac{1}{2}(\sigma_{1}^{2} + \tau^{2}) + \frac{\sigma_{1}\tau^{2}}{\sqrt{\sigma_{0}^{2} + \tau^{2}}} < \frac{(\sigma_{1} + \tau)^{2}}{2},$$

$$\frac{\sigma_{1}\tau^{2}}{\sqrt{\sigma_{0}^{2} + \tau^{2}}} < \sigma_{1}\tau,$$

$$\tau < \sqrt{\sigma_{0}^{2} + \tau^{2}},$$

The fact that S_0 and T are stochastically independent, and S_1 is a function of T implies that S_0 and S_1 are uncorrelated. Thus, under perfect observability finding 3 of the introduction cannot be obtained. Put differently, the possibility to transfer reputation from one generation of managers to the next crucially depends on the fact that T is not observable. The reputation of the firm can only affect expectations about the technology type if T is not perfectly known. Clearly, if it is revealed, reputation transfer is not an issue.

Note that the innovator's skill does not have a positive effect on the sales price of the firm. While this does not have negative welfare consequences in a setting in which S_0 is not a choice variable, it is clear that in a slightly extended setting in which innovators can initially invest in their managerial skills, there is less investment in this skill under perfect observability than under the setting considered in the previous section. We return to this issue in Section 4.3.

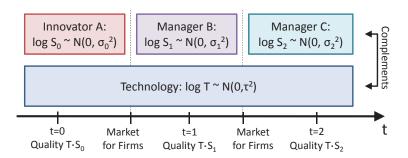
4.2 Additional Trading of Firms

In the previous section, we assumed that the firm is traded only before date t = 1. Firms with better signals $S_0 T$ had a better expected performance. Thus, due to imperfect observability and complementarity, they were bought by better managers. Because the signal about technology was noisy, the matching between managers and technologies was not perfect. As we show in this subsection, by introducing additional trading possibilities, the matching is improved and welfare increases. In our setting, the matching is efficient already after the second market for firms.

For a formal analysis, let us assume that there is a third class of managers, running firms at date t=2. Their types S_2 are lognormally distributed along $\log S_2 \sim N(0, \sigma_2)$. We solve the model using backward induction. On the market at the end of date t=1, the price P_1 for a firm will depends on expected future output, which

⁵Potentially, these managers could be the same as in period 1 but could be reallocated, such that $\sigma_2 = \sigma_1$.

Figure 7: Graphic Illustration of the Extension



again depends on observed qualities, thus $P_1(Q_0, Q_1)$. On the market at the end of date t = 0, the price P_0 depends on expected output in t = 1, the expected price at which the firm can be sold at date t = 1, both depending on the observed quality Q_0 , hence $P_0(Q_0)$. Let us start with the discussion of $P_1(Q_0, Q_1)$.

First, we show that $Q_1 = S_1 T$ perfectly reveals the type T of the technology. At the end of date t = 0, the quality $S_0 T$ is known, and because there is perfect matching between $S_0 T$ and S_1 , also type S_1 is known. Now at date t = 1, a quality $S_1 T$ is produced. Thus, the technology type T can then be perfectly inferred, $T = S_1 T/S_1$.

Formally, because $Q_0 = S_0 T$ and $Q_1 = S_1 T$ and $S_1 = Q_0^{\sqrt{\sigma_0^2 + \tau^2}}$, we obtain:

$$T = Q_0^{-\frac{\sigma_1}{\sqrt{\sigma_0^2 + \tau^2}}} Q_1. \tag{27}$$

The profit in period 2 of a manager of type S_2 buying a firm with technology T is

$$\Pi_2 - P_1(T) = S_2 T - P_1(T). \tag{28}$$

In equilibrium, the marginal expected profit must vanish,

$$S_2 - P_1'(T) = 0. (29)$$

Technology T is "designated" for type S_2 with

$$\log S_2 = \frac{\sigma_2}{\tau} \log T$$
, thus $S_2 = T^{\sigma_2/\tau}$, or $T = S_2^{\tau/\sigma_2}$. (30)

Substituting this into (29), considering that P(0) = 0 and solving the ensuing differential equation yields

$$P_1(T) = \frac{\tau}{\sigma_2 + \tau} T^{\frac{\sigma_2 + \tau}{\tau}} = \frac{\tau}{\sigma_2 + \tau} T^{\frac{\sigma_2 + \tau}{\tau}}.$$
 (31)

Thus, a manager of type S_2 makes an aggregate profit of $S_2 T - P_1(T) = \frac{\sigma_2}{\sigma_2 + \tau} S_2^{\frac{\sigma_2 + \tau}{\sigma_2}}$.

Now consider the market at the end of date t = 0. A firm that has produced quality Q_0 has a type T that is lognormally distributed with parameters as determined in (4) and (3). That implies that a manager of type S_1 , buying the firm, will get a price Π_1 as in (9) at date 1, then the quality $Q_1 = S_1 T$ will be revealed, and he will be able to sell the firm for a price

$$P_1(Q_0, Q_1) = \frac{\tau}{\sigma_2 + \tau} \left(Q_0^{-\frac{\sigma_1}{\sqrt{\sigma_0^2 + \tau^2}}} Q_1 \right)^{\frac{\sigma_2 + \tau}{\tau}} = \frac{\tau}{\sigma_2 + \tau} \left(Q_0^{-\frac{\sigma_1}{\sqrt{\sigma_0^2 + \tau^2}}} S_1 T \right)^{\frac{\sigma_2 + \tau}{\tau}}. \tag{32}$$

The cumulated profit is thus

$$\Pi_{1} + E[P_{1}(Q_{0}, Q_{1})] - P_{0}(Q_{0}) = \exp\left(\frac{\tau^{2} + \sqrt{\sigma_{0}^{2} + \tau^{2}} \sigma_{1}}{\sigma_{0}^{2} + \tau^{2}} \log Q_{0} + \frac{1}{2} \frac{\sigma_{0}^{2} \tau^{2}}{\sigma_{0}^{2} + \tau^{2}}\right)
+ E\left[\frac{\tau}{\sigma_{2} + \tau} \left(Q_{0}^{-\frac{\sigma_{1}}{\sqrt{\sigma_{0}^{2} + \tau^{2}}}} S_{1} T\right)^{\frac{\sigma_{2} + \tau}{\tau}}\right] - P_{0}(Q_{0})
= \exp\left(\frac{\tau^{2} + \sqrt{\sigma_{0}^{2} + \tau^{2}} \sigma_{1}}{\sigma_{0}^{2} + \tau^{2}} \log Q_{0} + \frac{1}{2} \frac{\sigma_{0}^{2} \tau^{2}}{\sigma_{0}^{2} + \tau^{2}}\right)
+ \frac{\tau}{\sigma_{2} + \tau} S_{1}^{\frac{\sigma_{2} + \tau}{\tau}} Q_{0}^{-\frac{\sigma_{1}}{\sqrt{\sigma_{0}^{2} + \tau^{2}}} \cdot \frac{\sigma_{2} + \tau}{\tau}}{T} E\left[T^{\frac{\sigma_{2} + \tau}{\tau}}\right] - P_{0}(Q_{0}), \tag{33}$$

where again T is lognormally distributed with parameters as in (4) and (3). Thus, $\ln T$ is normally distributed with mean (3) and standard deviation (4), and hence $\ln T^{\frac{\sigma_2+\tau}{\tau}}$ is normally distributed with $\frac{\sigma_2+\tau}{\tau}$ times the mean and $\frac{\sigma_2+\tau}{\tau}$ times the standard deviation. Hence, the expected value amounts to

$$E\left[T^{\frac{\sigma_2+\tau}{\tau}}\right] = \exp\left(\frac{\sigma_2+\tau}{\tau} \frac{\tau^2}{\sigma_0^2+\tau^2} \log Q_0 + \frac{1}{2} \frac{\sigma_2+\tau}{\tau} \frac{\sigma_0^2 \tau^2}{\sigma_0^2+\tau^2}\right). \tag{34}$$

Substituting into (33) and taking the derivative with respect to Q_0 , then substituting $S_1 \to Q_0^{\frac{\sigma_1}{\sqrt{\sigma_0^2 + \tau^2}}}$ and solving the ensuing differential equation yields

$$P_0(Q_0) = \frac{\tau^2 \left(\sqrt{\sigma_0^2 + \tau^2} - \sigma_1\right) - \sigma_0^2 \sigma_1}{\tau \left(\sigma_2 + \tau\right) \sqrt{\sigma_0^2 + \tau^2}} \exp\left(\frac{\sigma_0^2 \tau \left(\sigma_2 + \tau\right)}{2 \left(\sigma_0^2 + \tau^2\right)}\right) Q_0^{\frac{\tau \left(\sigma_2 + \tau\right)}{\sigma_0^2 + \tau^2}},\tag{35}$$

for $\sigma_1 < \tau^2/\sqrt{\sigma_0^2 + \tau^2}$. If this condition is not satisfied, then (formally) the price of firms becomes negative. The economic meaning is that worse managers want to buy better firms and there cannot exist a sorting equilibrium.

4.3 Moral Hazard (tbw.)

5 Conclusion

In the life cycle of a firm, an ownership change can be an incisive event, especially if new management is brought in. We have constructed a model of ownership change,

taking into account both the improved sorting that such a market provides and reputation considerations. Some background technology that is a complement in the production process works like a storage device for reputation. The noisier the type of the technology, the higher the correlation of types between initial innovators and managers will be, thus the better reputation transfer will work.

On the other hand, the variance between types of technologies also influences the prices paid in the market for firms. If the variance is extreme, this implies that good technologies differ a lot from bad ones. Hence, managers can benefit from paying a high price for firms. This may serve as an incentive for innovators to work hard, to drive up the price of their firm. Hence, creating a market for trading the firms' long term asset (i. e., their technology) benefits the efficient allocation of resources. The "reputation" of innovators partly determines the firm value due to imperfect observability.

References

- ABOWD, J., J. HALTIWANGER, J. LANE, K. MCKINNEY, AND K. SANDUSKY (2007): "Technology and Skill: An Analysis of Within and Between Firm Differences," NBER Working Paper No. 13043.
- ACHARYA, V., M. PAGANO, AND P. VOLPIN (2010): "Seeking Alpha: Excess Risk Taking and Competition for Managerial Talent," Working Paper, European Finance Association.
- Andersson, F. (2002): "Pooling Reputations," International Journal of Industrial Organization, 20(5), 715–730.
- Andersson, F., M. Freedman, J. Haltiwanger, and K. Shaw (2009): "Reaching for the Stars: Who Pays for Talent in Innovative Industries?," *Economic Journal*, 119(06), F308–F332.
- BAKER, G., M. GIBBS, AND B. HOLMSTRÖM (1993): "Hierarchies and Compensation," *European Economic Review*, 37(x), 366–378.

- Baker, G., and B. Holmström (1995): "Internal Labor Markets: Too Many Theories, Too Few Facts," *American Economic Review*, 85(2), 255–259.
- BAR-ISAAC, H. (2007): "Something to Prove: Reputation in Teams," RAND Journal of Economics, 38(2), 495–511.

- Gabaix, X., and A. Landier (2008): "Why Has CEO Pay Increased So Much?," *Quarterly Journal of Economics*, 123(1), 49–100.
- HAKENES, H., AND M. PEITZ (2007): "Observable Reputation Trading," *International Economic Review*, 48(2), 693–730.
- ——— (2008): "Umbrella Branding and the Provision of Quality," *International Journal of Industrial Organisation*, 26(2), 546–556.
- LEVIN, J., AND S. TADELIS (2005): "Profit Sharing and the Role of Professional Partnerships," Quarterly Journal of Economics, 120(1), 132–172.
- MORRISON, A. D., AND W. J. WILHELM (2004): "Partnership Firms, Reputation, and Human Capital," *American Economic Review*, 94(5), 1682–1692.
- TADELIS, S. (1999): "What's in a Name? Reputation as a Tradeable Asset," American Economic Review, 89(3), 548–563.
- ———— (2002): "The Market for Reputations as an Incentive Mechanism," *Journal of Political Economy*, 82(2), 854–882.